AP Calculus BC - Particle Motion Problems for Practice.

- 1. [1980 BC #1] The acceleration of a particle moving along a straight line is given by $a(t) = 10e^{2t}$.
 - a) Write an expression for the velocity v(t), in terms of t, if v(0) = 5.
 - b) During the time that the velocity increases from 5 to 13, how far does the particle travel?
 - c) Write an expression for the position x(t), in terms of *t* of the particle, if x(0) = 0.
- 2. [1986 BC #1] A particle moves along the *x*-axis so that at any time, its acceleration is given by $a(t) = \frac{1}{t}$. At time t = 1, the velocity of the particle v(1) = -2 and its position v(1) = 4.

position x(1) = 4.

- a) Find the velocity v(t) for $t \ge 1$.
- b) Find the position x(t) for $t \ge 1$.
- c) What is the position of the particle when it is farthest to the left? Justify your answer.
- 3. [1990 BC #1] A particle starts at time t = 0 and moves along the *x*-axis so that its position at any time $t \ge 0$ is given by $x(t) = (t-1)^3(2t-3)$.
 - a) Find the velocity of the particle at any time $t \ge 0$.
 - b) For what values of t is the velocity of the particle less than zero?
 - c) Find the value of *t* when the particle is moving to the left and the acceleration is zero.
- 4. [1991 BC#1] A particle moves on the x-axis so that its velocity at any time $t \ge 0$ is given by $v(t) = 12t^2 36t + 15$. At t = 1, the particle is at the origin.
 - a) Find the position x(t) of the particle for any time $t \ge 0$.
 - b) Find all values of *t* for which the particle is at rest.
 - c) Find the maximum velocity of the particle on $0 \le t \le 2$.
 - d) Find the total distance traveled by the particle from t = 0 to t = 2.